It has been suggested that a 'slow virus' may cause multiple sclerosis, and experiments on the possibility of transmitting the agent are continuing (Campbell, Norman, and Sandry, 1963; Dick, McAlister, McKeown, and Campbell, 1965; Field, 1966, 1968, 1969). Further, some circumstantial evidence suggests that the disease may be acquired in infancy even though the clinical manifestations appear much later (Millar, 1966; Dean, 1967; Kurtzke, 1968).

These two suggestions could be combined into a single, simple, and testable hypothesis which, if true, should logically result in the 'clustering' (i.e., groups of cases closely associated in time and place) of cases by date and place of birth simultaneously. This paper reports the results of an investigation of the temporal-spatial distribution of multiple sclerosis in Northern Ireland. The statistical techniques used are basically those described by Ederer, Myers and Mantel (1964) and by David and Barton (1966).

DATA

ASCERTAINMENT

Since 1948, efforts have been made to ascertain all cases of multiple sclerosis in Northern Ireland and a central register of all the ascertained cases (living and dead) has been compiled. On 1 October 1968, there were 1,418 cases on the register. Most of them were ascertained through a countrywide prevalence survey in 1949–53 (Allison and Millar, 1954). The remainder have been ascertained since 1954, mainly by these two consultant neurologists, through general practitioner referrals, consultant clinics, hospital records, and post-mortem reports. In the absence of any specific diagnostic test it is not possible to estimate the degree of ascertainment that has been achieved. However, the structure and administrative arrangements of the Health Service in Northern Ireland are such that, using the combination of methods listed above and the diagnostic criteria of Allison and Millar (which were adopted by the World Federation of Neurologists for epidemiological studies (Allison, 1960)), very few cases are likely to have been missed.

The place and year of birth of patients are among the data routinely obtained in the course of ascertainment. These were extracted from the patients' records, and in the few cases where they had not been recorded, the information was obtained by means of a postal survey conducted among the surviving cases.

MULTIPLE SCLEROSIS CASES STUDIED

From the total of 1,418 cases, two groups, A and B, were selected for this investigation.

Group A comprised all 783 patients born within the area now known as Northern Ireland during the years 1901–25. This period was chosen as multiple sclerosis manifests itself mainly between the ages of 20 and 40 years (Brain, 1966; Acheson, 1965). Consequently, many individuals born after 1925 and destined to develop the disease would not have manifested it at the time of this investigation. In addition some multiple sclerosis patients born before 1901 would have died before 1948 (the year in which ascertainment began) and were therefore missed. Finally, the data necessary for the valid application of the method of Ederer et al. (1964) were available on all group A cases.

For the application of the method of David and Barton (1966) a more circumscribed group of cases with more detailed information is desirable. Accordingly, a sub-group B, of group A, comprising 109 multiple sclerosis patients born in Northern Ireland during 1921–25 whose exact day of birth could be traced, was selected.
METHODS

The two statistical techniques employed have been used widely in recent years to study the space-time distributions of relatively rare diseases, particularly leukaemia (Ederer et al., 1964; Ederer, Myers, Eisenberg, and Campbell 1965; Barton, David, and Merrington, 1965; Lock and Merrington, 1967; Merrington and Spicer, 1969). They require, therefore, no detailed description here and only their application to the present data is presented.

METHOD OF EDERER et al. (1964)

The method of Ederer et al. (1964) requires a priori the definition of the space-time units to be used. In general, a space-time unit will consist of a suitably defined area studied for a period of time. The most suitable space-time units derivable from the data available were the administrative areas and geographical areas shown in the Figure, each studied for the period of one calendar year. Both administrative and geographical units were used because morbidity and mortality data are normally handled on an administrative basis, although in physical terms the spread of infectious diseases is more likely to follow the geographical contours of the country. Administratively, Northern Ireland was considered to consist of seven rather than eight areas—Londonderry County Borough and Londonderry County were studied as one area. The geographical areas shown in the Figure are based on the Ordnance Survey map of Northern Ireland, the tenth area is Belfast. The time interval of one calendar year was selected because, for most of the cases, only the year of birth was known.

To eliminate the effects of possible time trends in the number of cases born in a particular area and for computational convenience the period 1901–25 was divided up into five non-overlapping quinquennial periods, 1901–05, 1906–10, 1911–15, 1916–20 and 1921–25. From these divisions 5 × 7 = 35, five-year administrative units* and 5 × 10 = 50, five-year geographical units were obtained. Thus, each of these larger units comprised five of the appropriate calendar year space-time units defined above. The relevant data together with $K$, the total number of cases occurring in any five-year unit, are presented in Tables I and II.

The statistics $m_1$ and $m_0$, defined respectively as the observed maximum number of cases occurring in any one year of a five-year unit and the observed maximum number of cases occurring in any two consecutive years of a five-year unit, were employed as indices of clustering. For example, the values of $m_1$, $m_0$, and $K$ for the quinquennium 1901–05 in area 10 are 12, 20, and 42 respectively (Table II).

The null hypothesis that the numbers of cases occurring in each five-year unit were randomly distributed was tested. The test statistic proposed by Ederer et al. (1964) is a continuity corrected $x^2$ with one degree of freedom, defined as,

$$x^2 = \frac{\left( \sum m_1 - \sum m_0 \right) - 0}{\sum \sigma_1}$$

*Where there is no ambiguity, space-time unit has been abbreviated to unit.
where, for a particular five-year unit, \( \mu_1 \) is the expected value (hereafter denoted by \( E \)) of \( m_1 \) given \( K \) and \( \sigma_1^2 \) is the variance (hereafter denoted by \( VAR \)) of \( m_1 \) given \( K \), the summation extending over all admissible five-year units. The parameters \( \mu_2 \) and \( \sigma_2^2 \) are obtained from the conditional probability distribution of \( m_2 \) given \( K \) by a method credited to Feller (1957) and detailed in the appendix. Although equation (1) may be used as a test criterion for \( m_2 \) by substituting \( m_1, \mu_2, \) and \( \sigma_2^2 \) with \( m_2, \mu_2 \) and \( \sigma_2^2 \), these latter parameters cannot be obtained directly by Feller's method.

As \( K \) becomes large the generation of the exact occupancy distribution of each five-year unit on the computer becomes lengthy. However, the computing time may be substantially reduced by estimating the parameters \( \mu_1, \sigma_1^2, \mu_2, \) and \( \sigma_2^2 \) using quasi-occupancy distributions generated by Monte Carlo methods (Naylor, Balintfy, Burdick, and Chu, 1966). This approach was adopted for the estimation of the parameters \( E(m_1/K) \) and \( VAR(m_1/K) \) for \( K > 35 \), in addition to \( E(m_2/K) \) and \( VAR(m_2/K) \)

for all \( K \). As the estimation procedure involved 1,000 simulated trials, the degree of approximation was small and the reliability of the test criterion was not affected.

Using this technique, Ederer et al. (1965) have demonstrated the clustering of cases of poliomyelitis and infectious hepatitis in Connecticut.

**METHOD OF DAVID AND BARTON (1966)**

The David and Barton (1966) space-time interaction test, which was used to analyse group B cases, treats the space co-ordinates as a randomization set and postulates that all possible allocations of a given time to a given space point are equally likely. The statistical test criterion used is the ratio of the average squared distance between space points within time clusters to the overall average. This method, therefore, unlike that proposed by Knox (1963), does not require a definition of a unit of distance but does require divisions of time to be made prior to the analysis. Where the incubation period of a particular disease is known, the interval of time chosen may be logically based on such knowledge, but where such a period is unknown, as it is here, the selection must be arbitrary.
TABLE III
DISTRIBUTION OF 199 ASCERTAINED MULTIPLE SCLEROSIS CASES BORN IN NORTHERN IRELAND, 1921-25 (GROUP B)

<table>
<thead>
<tr>
<th>Year of Birth</th>
<th>Cases Traced and Analysed</th>
<th>Cases Not Traced</th>
<th>All Ascertained Cases</th>
</tr>
</thead>
<tbody>
<tr>
<td>1921</td>
<td>28</td>
<td>7</td>
<td>35</td>
</tr>
<tr>
<td>1922</td>
<td>25</td>
<td>8</td>
<td>33</td>
</tr>
<tr>
<td>1923</td>
<td>19</td>
<td>10</td>
<td>29</td>
</tr>
<tr>
<td>1924</td>
<td>17</td>
<td>6</td>
<td>23</td>
</tr>
<tr>
<td>1925</td>
<td>20</td>
<td>7</td>
<td>27</td>
</tr>
<tr>
<td>Total</td>
<td>109 (74%)</td>
<td>38 (26%)</td>
<td>147 (100%)</td>
</tr>
</tbody>
</table>

The exact day of birth, required for this test, was successfully obtained in 109 (74%) of the 147 cases born during 1921-25 (Table III). The space coordinates (x, y) of the place of birth of these cases were taken from the Ordnance Survey map, 3rd series (Ashitey, 1969). These were arranged consecutively in time order and divided into time groups using each of the time intervals, 8 days, 18 days, 31 days, 41 days, 51 days, and 61 days. The test criterion Q was calculated for each time interval using a computer programme kindly supplied to us by Dr. Maxine Merrington.

This test criterion has previously been used to show clustering of cases of measles and of poliomyelitis but not of acute leukaemia (Barton et al., 1965).

RESULTS

GROUP A CASES

Pertinent results are summarized in Table IV. No significant results were obtained, the calculated values of $x^2$ for both administrative and geographical 5-year units being less than the usually acceptable value (3.84) for one degree of freedom. The generally small deviation from expectation obtained, particularly for geographical divisions, may be indicative of a mechanism leading to a quinquennium to quinquennium uniformity in the maximum number of people in one year who were born in those areas and subsequently developed the disease. It was therefore concluded, on the evidence afforded by these data, that multiple sclerosis cases in Northern Ireland were not clustered, by their year and place of birth simultaneously, during the period investigated.

TABLE V
RESULTS OF ANALYSIS OF GROUP B CASES USING METHOD OF DAVID AND BARTON (1966)

<table>
<thead>
<tr>
<th>Interval between Time Clusters (days)</th>
<th>No. of Clusters</th>
<th>$Q$</th>
<th>$d^*$</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>70</td>
<td>0.79</td>
<td>-1.70</td>
</tr>
<tr>
<td>18</td>
<td>42</td>
<td>0.93</td>
<td>-0.96</td>
</tr>
<tr>
<td>31</td>
<td>13</td>
<td>0.97</td>
<td>-0.61</td>
</tr>
<tr>
<td>41</td>
<td>7</td>
<td>0.98</td>
<td>-0.83</td>
</tr>
<tr>
<td>51</td>
<td>5</td>
<td>0.99</td>
<td>-0.31</td>
</tr>
<tr>
<td>61</td>
<td>4</td>
<td>0.99</td>
<td>-0.73</td>
</tr>
</tbody>
</table>

* $d^* = (Q - 1)/S.E. of Q

GROUP B CASES

Table V shows the values of the test criterion Q obtained for the time intervals studied. Assuming that Q is approximately normally distributed, $d^*$ may be referred to the normal probability scale. Since none of the d values is less than -2 (David and Barton, 1966), it was concluded that the null hypothesis cannot be rejected, i.e., there is no significant evidence of clustering of the multiple sclerosis cases studied by this method.

DISCUSSION AND CONCLUSION

The results of the present investigation provide no evidence for the rejection of the null hypothesis that multiple sclerosis cases in Northern Ireland were randomly distributed by date and place of birth simultaneously. It should be emphasized that this finding must be viewed against the assumption that the disease is acquired in infancy as well as the statistical techniques employed.

With the method of Ederer et al. (1964), the spacetime units chosen are an integral part of the hypothesis tested, and consequently the results obtained would not necessarily be valid for units defined differently from those employed here. While the degree of completeness of ascertainment of cases would influence the results, the data used were thought to be reliable.

TABLE IV
RESULTS OF ANALYSIS OF GROUP A CASES BY METHOD OF EDERER ET AL. (1964)

<table>
<thead>
<tr>
<th>Area</th>
<th>No. of 5-year Units</th>
<th>No. of 5-year Units with Two or More Cases</th>
<th>Analysis of Index $m_1$</th>
<th>Analysis of Index $m_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>$\Sigma m_1$</td>
<td>$E(\Sigma m_1)$</td>
</tr>
<tr>
<td>Administrative</td>
<td>105</td>
<td>35</td>
<td>252</td>
<td>244.15</td>
</tr>
<tr>
<td>Geographical</td>
<td>50</td>
<td>49*</td>
<td>254</td>
<td>254.23</td>
</tr>
</tbody>
</table>

*One geographical 5-year unit (Table II) had zero cases and was omitted from the analysis.
The method of David and Barton (1966) has the property of testing interaction whilst being substantially unaffected by irregularities of the separate time and space distributions. This, of course, is an advantage where ascertainment is incomplete or where cases are geographically clustered in towns and villages. In this investigation 109 of the 147 known cases born between 1921 and 1925 could be included in the analysis. However, there appears to be no obvious reason why these omissions should obscure rather than magnify any clustering that might have occurred.

Although the demonstration of clustering of cases would have provided an important piece of evidence in support of the hypothesis that multiple sclerosis is due to a 'slow virus' infection acquired in infancy, other factors including infectious bacteria, radiation, poisons, etc., may also give rise to clusters of cases. Similarly, the present negative result is not conclusive, by itself, in excluding a viral aetiology, since if the 'virus' is endemic and common, then the people affected by it might be randomly distributed. This latter possibility is unlikely to be true of multiple sclerosis which is relatively rare; but matters may be complicated further by postulating a causative virus which attacks many people, with only a fraction of them developing a neurological complication, as in the case of measles. However, the absence of clustering of cases by date and place of birth simultaneously is interesting because it supports other epidemiological work (Ashitey and Millar, 1970) which suggests that if the disease is acquired in infancy or even in adolescence, then the aetiological factor does not exhibit 'epidemic' characteristics.

**SUMMARY**

An investigation was carried out into the time-space clustering of cases of multiple sclerosis, using the date and place of birth of affected persons. Altogether 783 ascertained cases born in Northern Ireland during the period 1901–25 were studied by two statistical techniques. No clustering of cases was detected. The significance of the results is discussed.

We thank Dr. J. H. D. Millar and Dr. R. S. Allison for allowing us to study their records; Dr. Maxine Merrington, Department of Statistics, University College, London, for the computer programme for the David and Barton (1966) test; the computing laboratory of Queen's University, Belfast, for facilities, and Mrs. Eileen MacKenzie for secretarial assistance. Finally, we are grateful to Professor Peter Foggatt for his advice and helpful criticism during the study and in the preparation of this paper.

**REFERENCES**


φ: 568 5 weights 1568.4

G. AMARH ASHITEY AND GILBERT MACKENZIE


APPENDIX

The following method due to Feller (1957) was used in the present investigation to obtain the conditional probability distribution \( m_1 \), when \( K \), the total number of cases occurring in any five-year unit, was less than or equal to 35. For values of \( K \) beyond 35, recourse to Monte Carlo methods is necessary in order to avoid excess processor time.

Feller's formula for \( n (=5) \) years, and where the cells are arranged in descending order of occupying cases \( k_1, k_2, \ldots, k_5 \), is

\[
P(k_1, k_2, \ldots, k_5) = \frac{5!}{K!} \left( \frac{7}{j!} \right)^k \times 5^{-K}
\]

where \( n_j (j = 0, \ldots, K) \) is the number of years containing exactly \( j \) cases, and \( k \) \((i = 1, \ldots, 5)\) is the \( i \)th occupancy number.

Since the occupancy numbers have been arranged in descending order of occupying cases, \( m_1 \) is identically equal to \( k_1 \). Thus, denoting the conditional probability distribution of \( m_1 \) given \( K \) by \( P(m_1/K) \), the first two moments about the mean of this distribution, \( \mu_1 \) and \( \sigma^2_1 \), may be computed by definition, i.e.,

\[
\mu_1 = \Sigma m_1 P(m_1/K)
\]

\[
\sigma^2_1 = \Sigma m_1^2 P(m_1/K) - \mu_1^2
\]

where in each case the summation extends over the admissible range of \( m_1 \) values, such that \( \Sigma P(m_1/K) = 1 \).
at variance with this is the finding of Cartwright and Ward (1968), who asked about the family planning advice offered by 232 general practitioners in Sheffield, England. They found a significantly greater response (90% v. 73%) to a short as opposed to a longer questionnaire. However, the questionnaires differed appreciably in content and precision of required responses.

There were two components to 'personalization': stamping vs. franking and verbal personalization. With respect to the former, Scott (1961) found a difference in favour of the stamp (93.3% vs. 89.2%), statistically significant on the large numbers in his study. Robinson and Agasim (1951) found a significant difference in favour of the stamp (73.8% v. 66.3%), but it is not clear that the study groups were comparable. They also found that the difference resulted from a poor return of franked envelopes from small towns where many of the franked were covered by a stamp. Clausen and Ford (1947), on the other hand, in a small study (no details given) reported no difference in response with stamped vs. franked envelopes. There may be an advantage to stamping rather than franking but it is probably small. With respect to verbal personalization Clausen and Ford (1947) found no difference in response between veterans receiving a letter with an inside address and personal salutation and comparable veterans receiving the same letter with no inside address and the salutation 'Dear Veteran'. The present data do not allow separation of the effects of stamping from verbal personalization but they strongly suggest no appreciable difference in personal v. impersonal as used.

It seems reasonable to conclude that the 'instrument' (the form of the letter, its accouterments and enclosures) makes little difference in response. It also seems that when a specific characteristic of the instrument is associated with differing response rates (e.g., the presence of the question on schooling) it is largely due to one subgroup of recipients (the Worcester elderly). Cartwright (1964) found that the addition of a question on schooling to a one-item questionnaire on hospitalization reduced response from 93.6% to 90.7%. It is not stated whether the lower figure was due to a particularly low response from a sub-segment of the population, e.g., the elderly.

Both the present studies show a decreasing response with increasing age. The second study suggests also that the social class of the recipient is important as Newton is a rather prosperous suburb of Boston whereas Worcester is a large city with a cross section of social classes. Neither conclusion is original but they have not been clearly documented in the past.

The value of the present studies lies in their placing in perspective the relative importance of the instrument and the characteristics of the target population in determining response. This is not to say that elderly or lower social class persons would always respond poorly—perhaps questionnaires concerned with matters other than health and disease would elicit a reversal of these findings. Nonetheless, it seems that money and effort spent in personalizing and 'improving' a mail instrument may not yield comparable improvement in response rate.

**Summary**

Two studies of the determinants of response rates of Massachusetts women to postal questionnaires are described. They suggest that the characteristics of the target population are more important than the instrument in determining response rate.

We are indebted to Dr. Jacob Feldman for advice. This work was supported by Program Project Grant 2-P01-CA06373 from the National Cancer Institute, United States Public Health Service.

**REFERENCES**


